



TOHOKU  
UNIVERSITY

# ***Multi-Objective Design Exploration (MODE) and Its Applications***

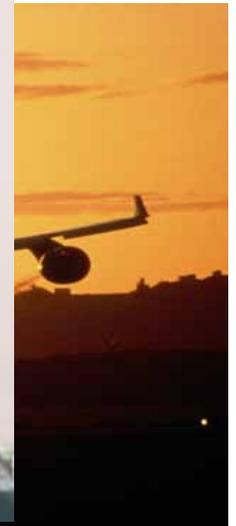
**Shigeru Obayashi**

*Institute of Fluid Science, Tohoku University*

東北大学流体科学研究所

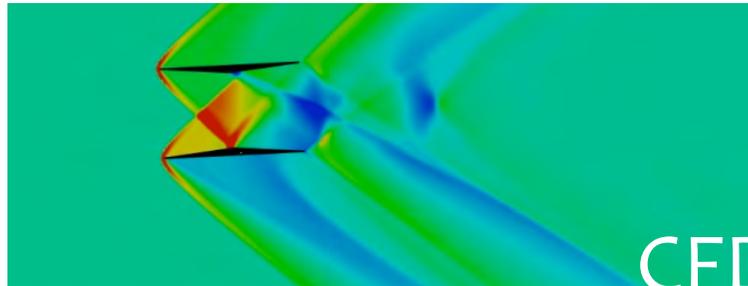
大林 茂

# *100 Years of Powered Flight*

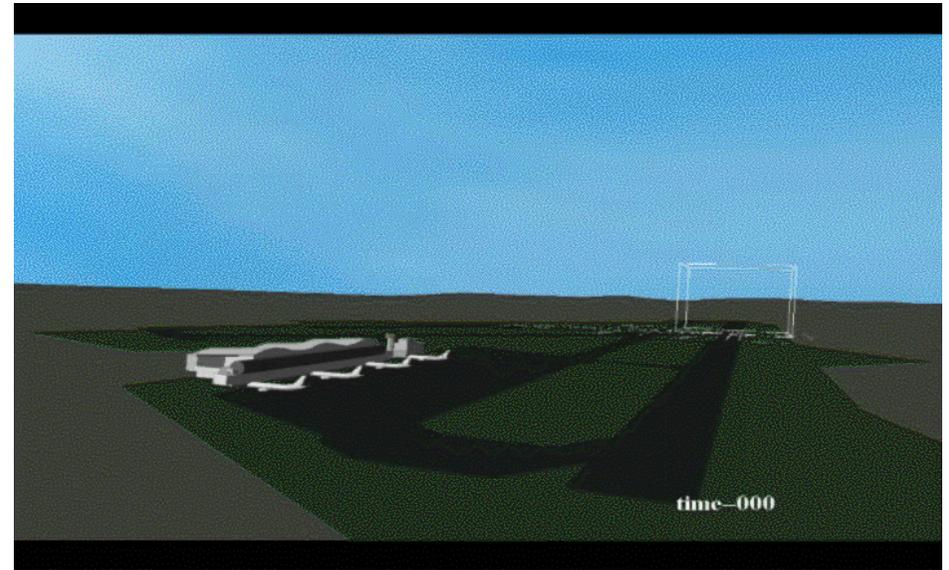


# Research Topics in Laboratory

## 1. Supersonic Biplane



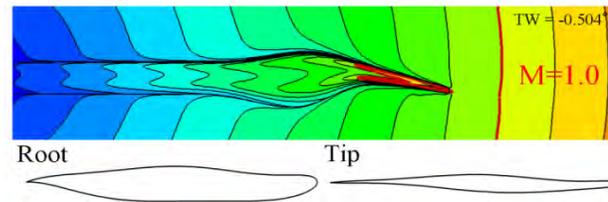
## 3. Measurement-Integrated Simulation



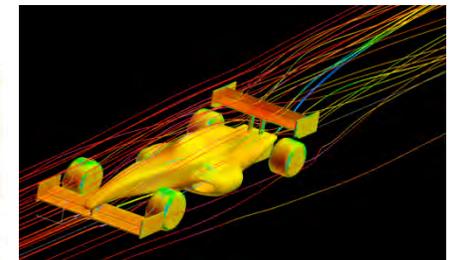
## 2. Multi-Objective Design Exploration (MODE)



Mitsubishi Regional Jet (MRJ)

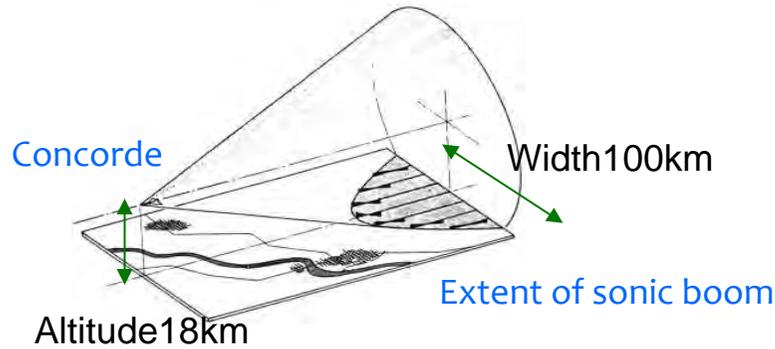


Helicopter Blade



Racing Car

# Mitigation of Sonic Boom



**Sonic boom noise is a bottleneck in the development of the next generation SST**

environmental standard for 2016~2019

Conventional Low Boom Technology

Approx. 30% Reduction of sonic boom

Axisymmetric linear theory

1. Rounded nose shape
2. Slender body

Innovative Low Boom Technology

100% reduction in linear theory!

Supersonic biplane theory

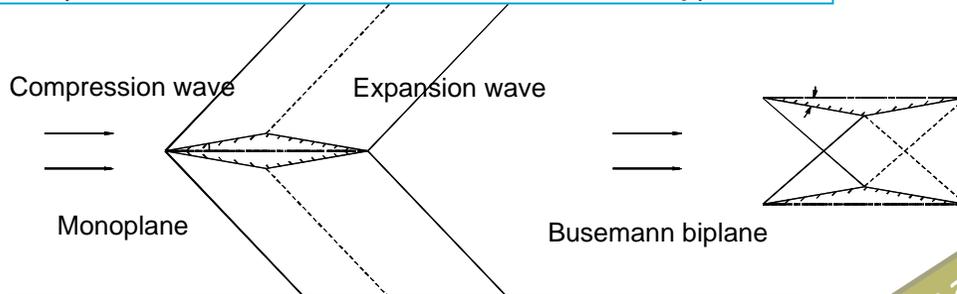
- Busemann biplane!



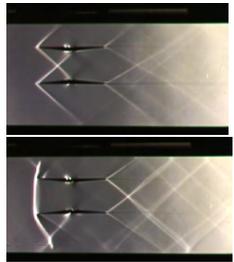
Breakthrough for larger SST

# Development of Supersonic Biplane Theory

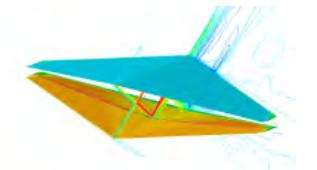
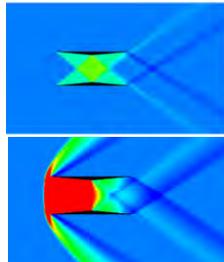
Busemann airfoil that cancels sonic boom (1930s)  
(limited to two-dimensional linear theory)



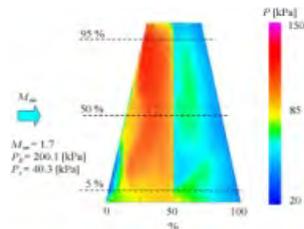
Research of supersonic biplane started from 2003 for the realization of silent SST



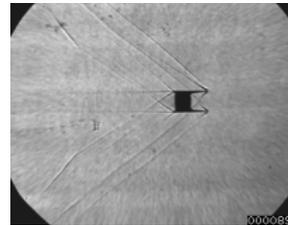
Investigation using EFD and CFD



CFD for Three-dimensional biplane



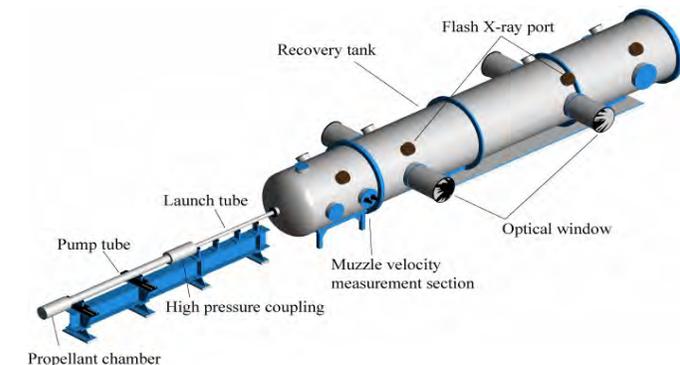
PSP measurement of three-dimensional shock interference



Ballistic-range supersonic free flight experiment (model size: 25mm)



Low speed radio controlled flight experiment



Evaluation of non-linearity and three-dimensionality of sonic boom on the ground

From airfoil theory to aircraft

**Aircraft Integration**  
Unsteady CFD Simulation,  
Supersonic wind tunnel experiment

**Sonic boom ground experiment**  
Supersonic free flight experiment  
(model size: 50mm)

# Measurement-Integrated Simulation of Atmospheric Turbulence

- Uncomfortable shake of aircraft
- Operational error
- Sometimes serious accidents

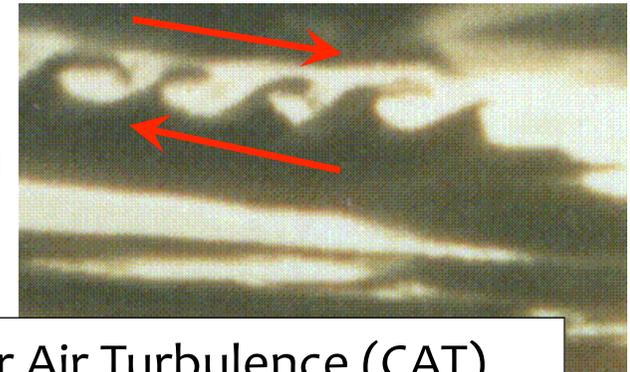
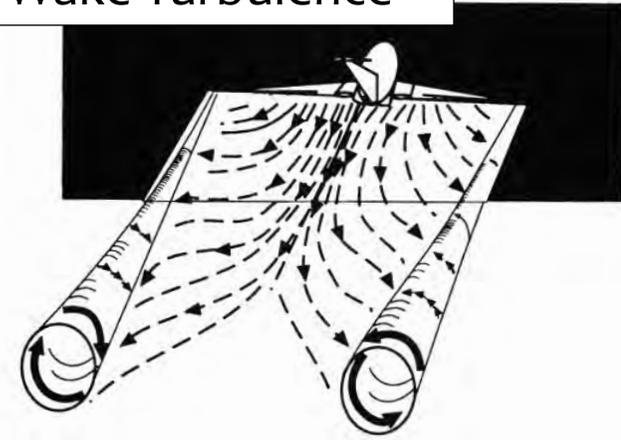
Thunderstorm



Mountain Wave



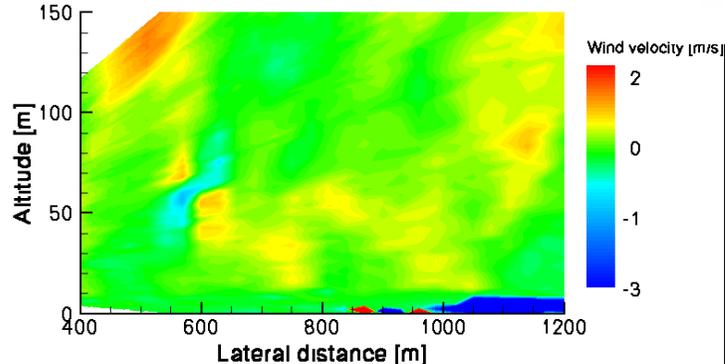
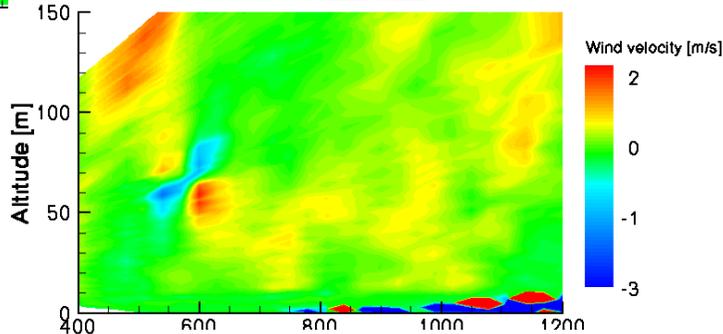
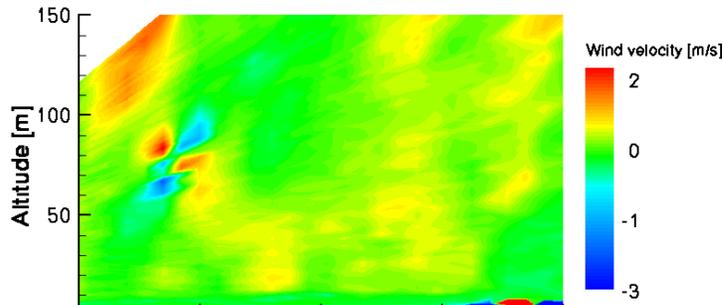
Wake Turbulence



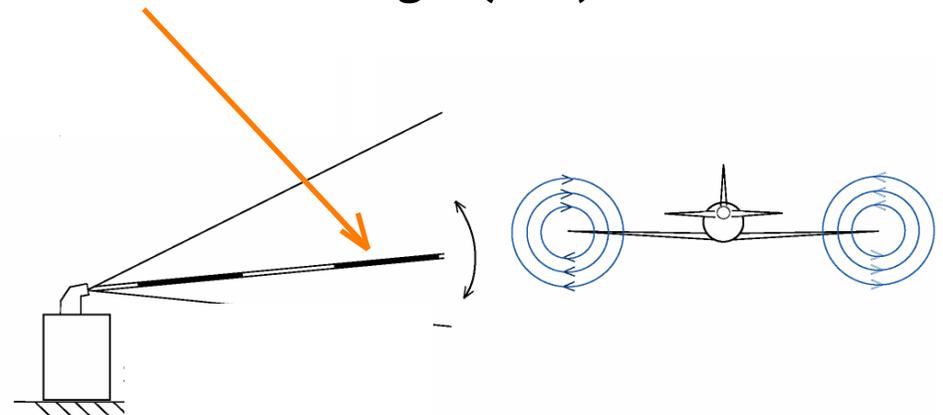
Clear Air Turbulence (CAT)

# Measurement of Wake Turbulence

## ➤ Lidar measurement at Sendai airport



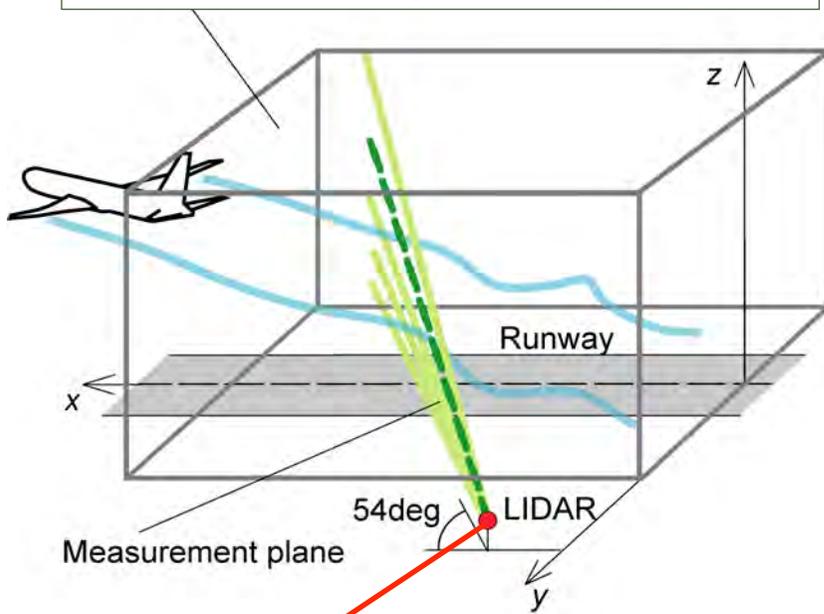
- Real-time measurement and visualization
- High resolution in elevator angle direction
- **30m resolution in line of sight (LOS) direction**



➤ **Lack of spatial resolution and 3D information!!**

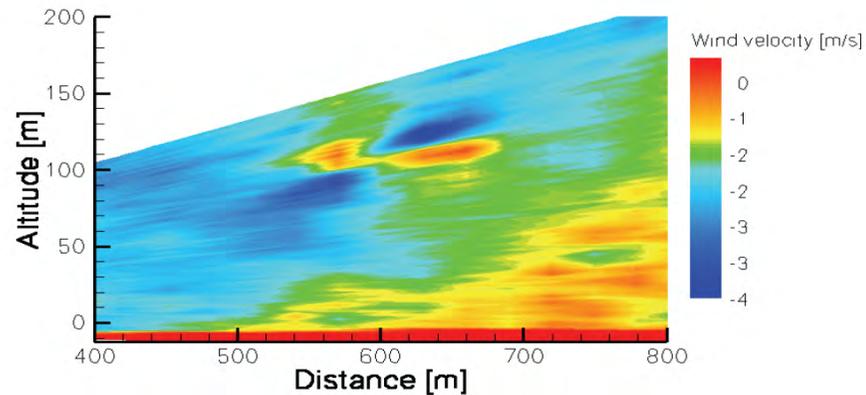
# Integrated-Simulation at Sendai Airport

Reproduce realistic wake vortices in supercomputer



Lidar (ENRI)

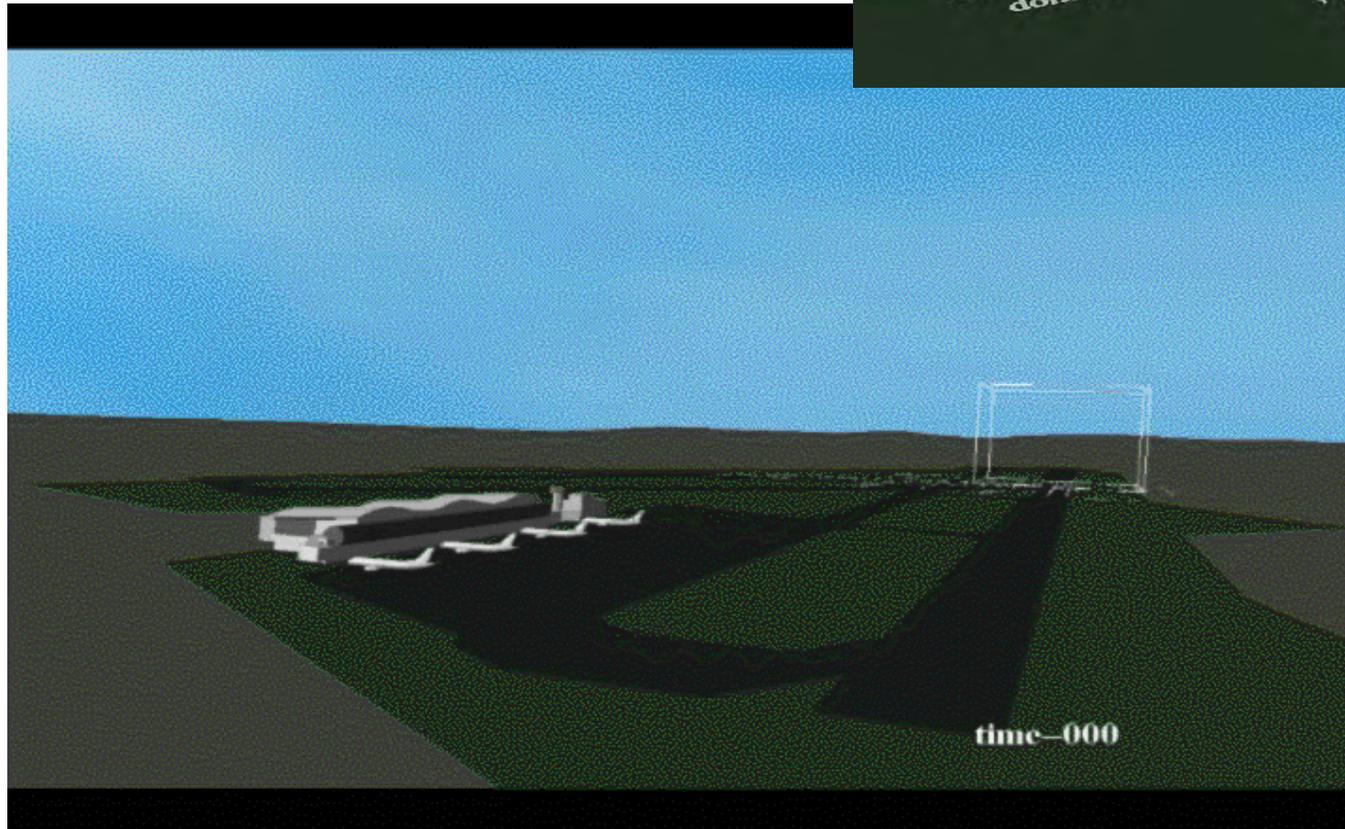
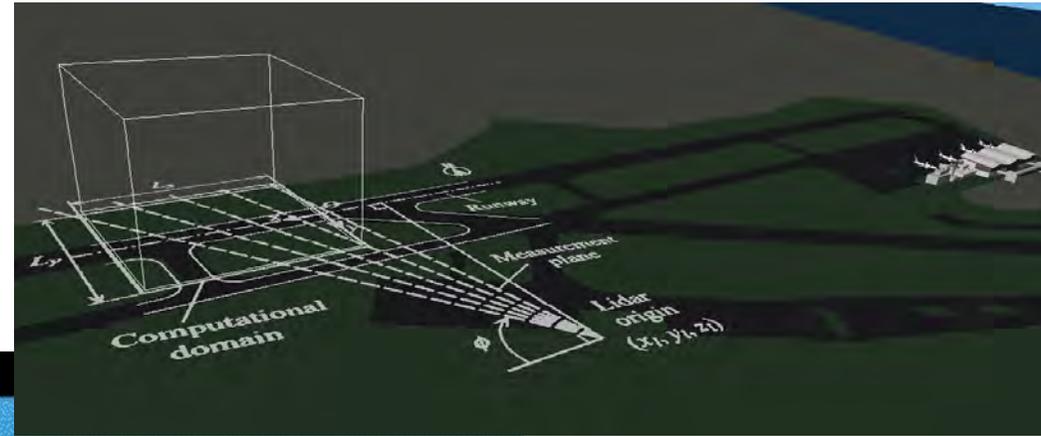
Data assimilation using four-dimensional variational method (4D-Var)



Lidar measurements of departing aircraft at Sendai airport

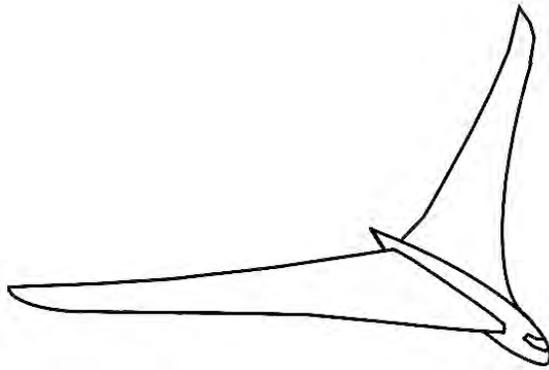
# Wake Turbulence at Sendai Airport

- ✓ Reproduced flow field is superimposed on the virtual reality model of Sendai airport

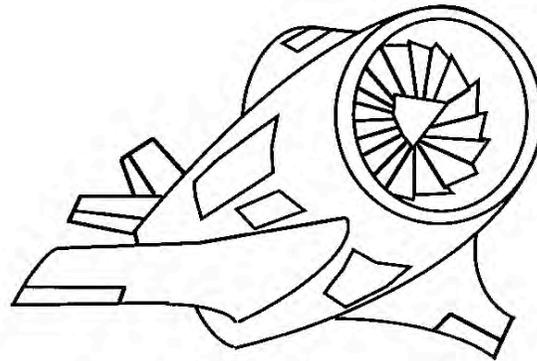


## Multidisciplinary Design Optimization (MDO) for Regional Jet

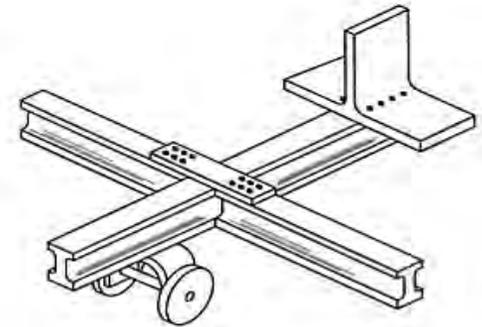
- Multi-Objective Design Exploration (MODE)
  - SOM
- R&D Project and Resulting MRJ
- Applications to Regional-Jet MDO Problems
  - Wing-body configuration
  - Wing-nacelle-pylon-body configuration
  - Winglet design
  - Horizontal tail structural design
- Lessons Learned



Aerodynamics



Propulsion

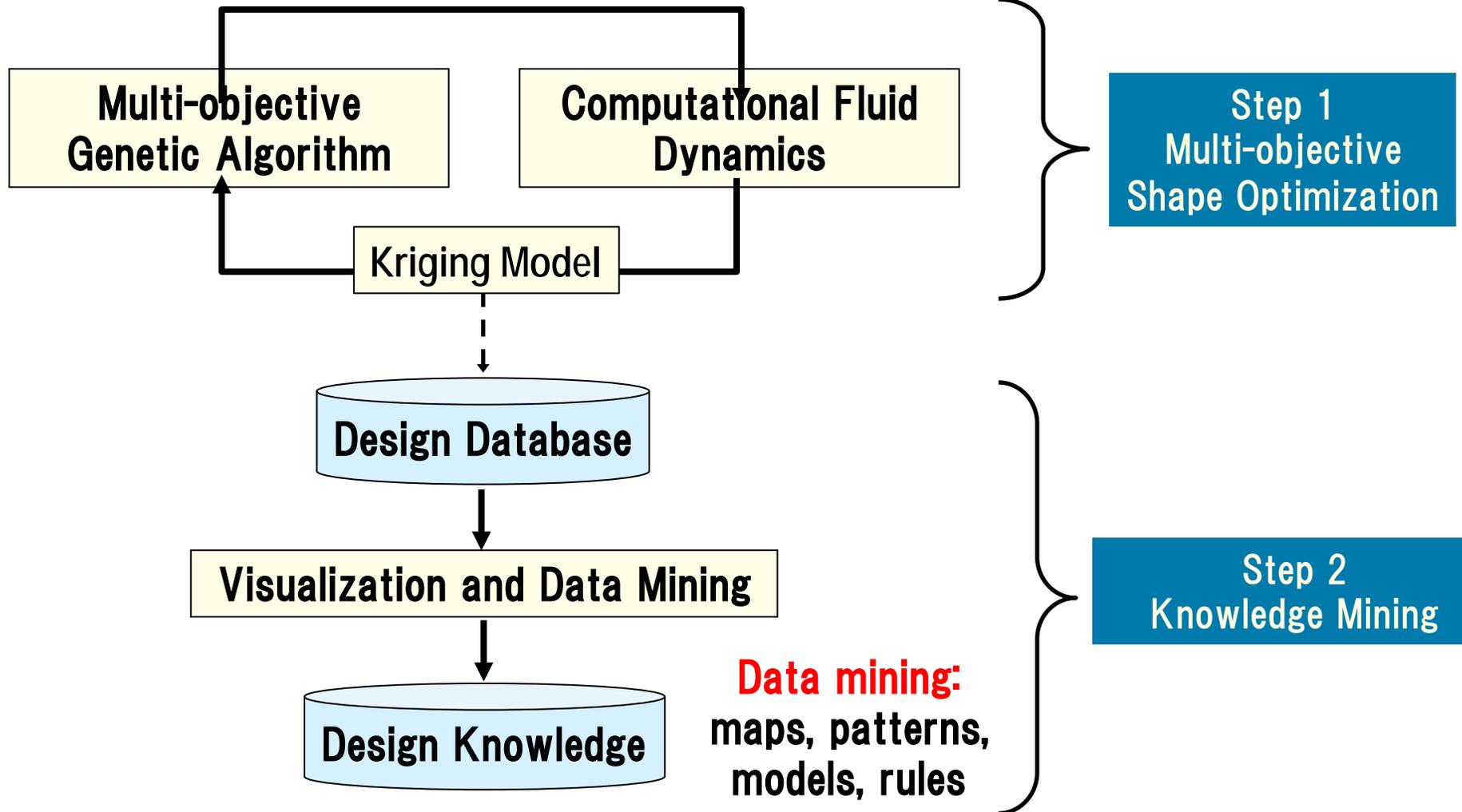


Structure

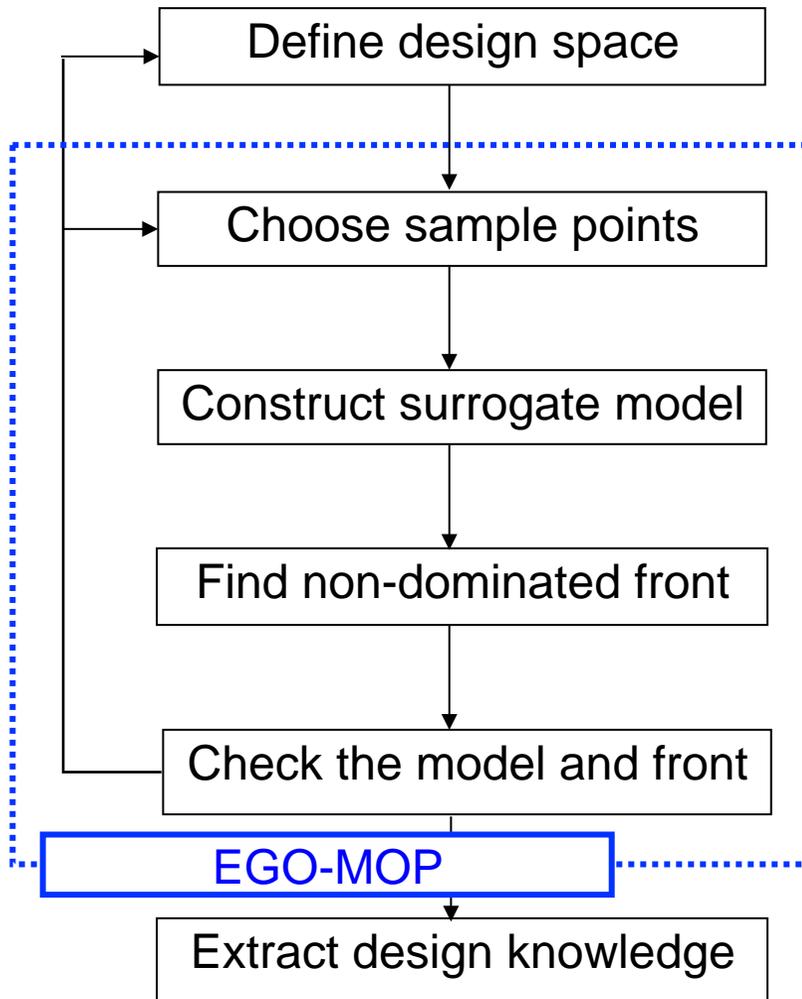
- Compromise of all disciplines
- **Multidisciplinary Design Optimization (MDO)**  
as **Multi-Objective Optimization (MOP)**

# MODE to Solve MOP

## Multi-Objective Design Exploration (MODE)



# Incorporating *EGO* to *MODE*



Parameterization: PARSEC, B-Spline, etc.

Design of Experiment: Latin Hypercube

EGO-MOP Using Kriging Model

Optimization: Evolutionary Algorithms (Genetic Algorithms)

Uncertainty Analysis: Expected Improvement based on Kriging Model, statistics of design variables, etc.

Data Mining: Analysis of Variance, Scatter Plot Matrix, Self-Organizing Map, Rough Set, etc.

# *Present MDO Problems*

1. Wing-body configuration
2. Wing-nacelle-pylon-body configuration
3. Winglet design
4. Horizontal tail structural design



# Optimization of Wing-Body Configuration

## Objective functions

### Minimize

1. **Drag** at the cruising condition
2. **Drag divergence** between the cruising and off-design condition
3. **Pitching moment** at the cruising condition
4. **Structural weight** of main wing

### ✓ Function evaluation tools

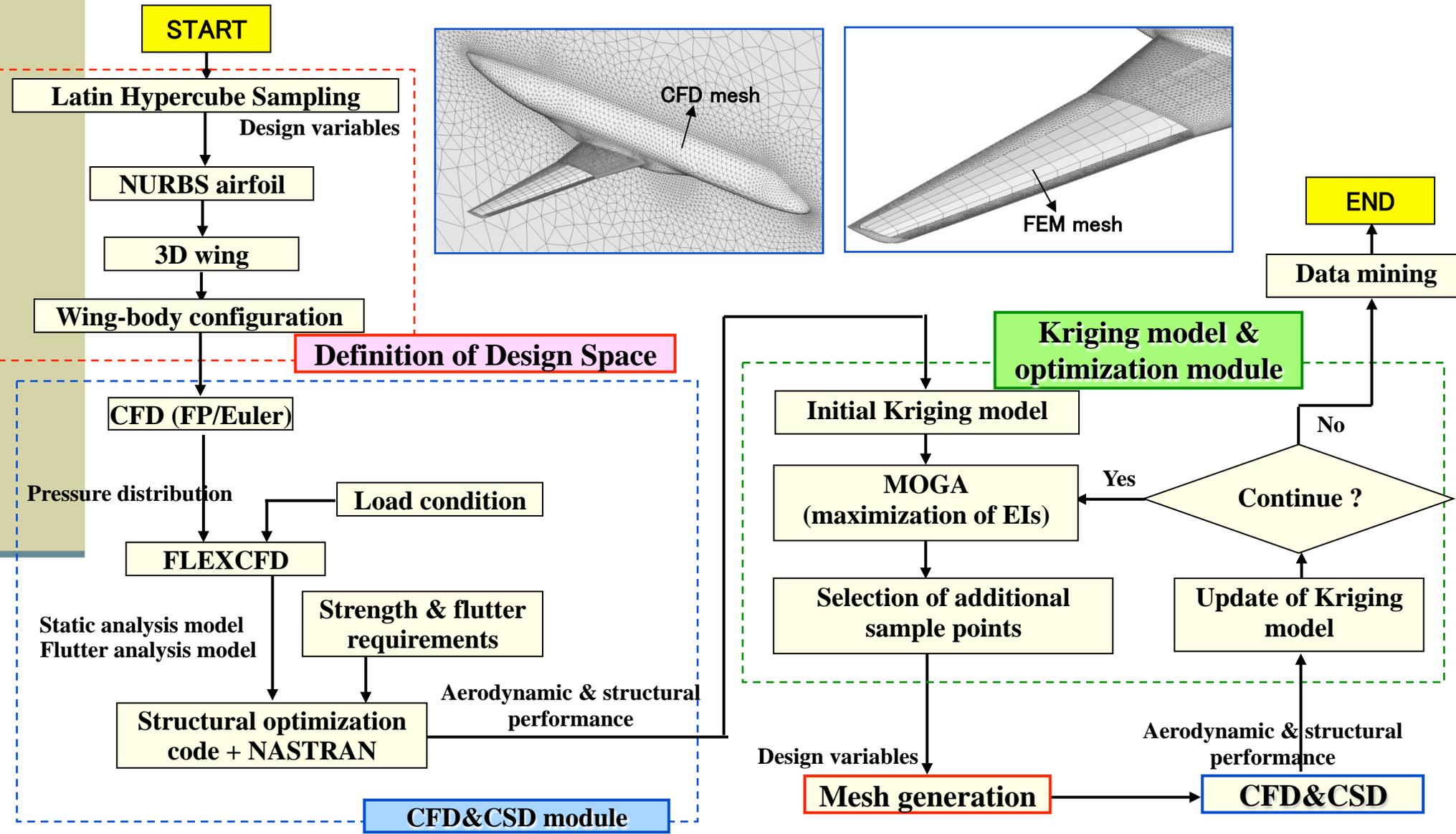
- CFD: Full Potential code (MHI in-house), Euler code (TAS-code)
- CSD/Flutter analysis: MSC. NASTRAN

## Design variables

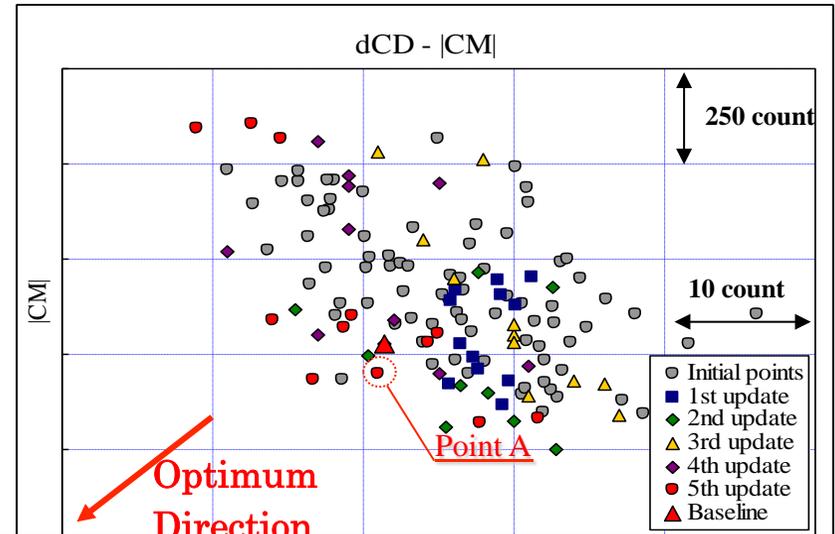
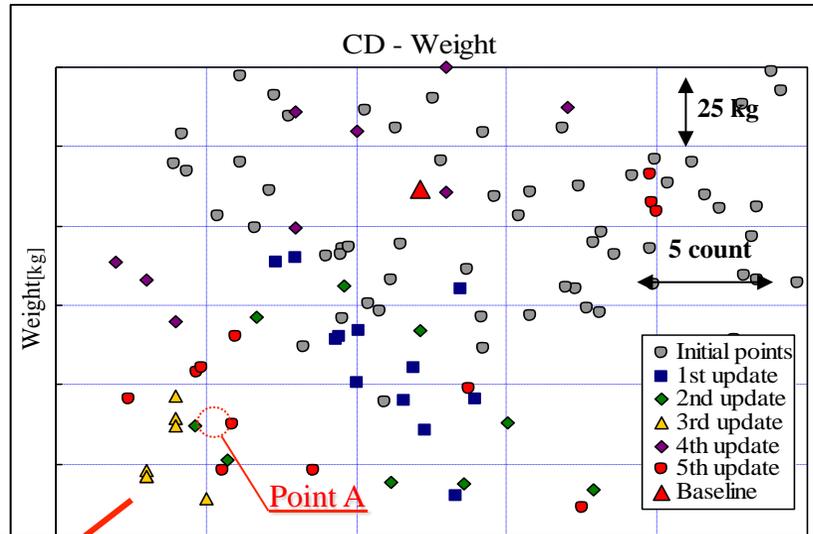
- Airfoil shapes at 4 spanwise sections ( $\eta = 0.1, 0.35, 0.7$  and  $1.0$ )  
→ 26 variables (NURBS)  $\times$  4 sections = 104 variables
- Twist angles at 5 sections = 5 variables

109 variables in total

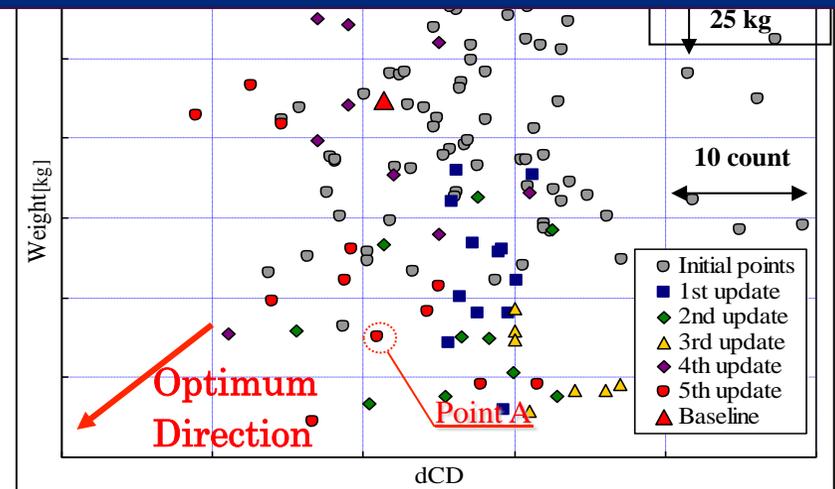
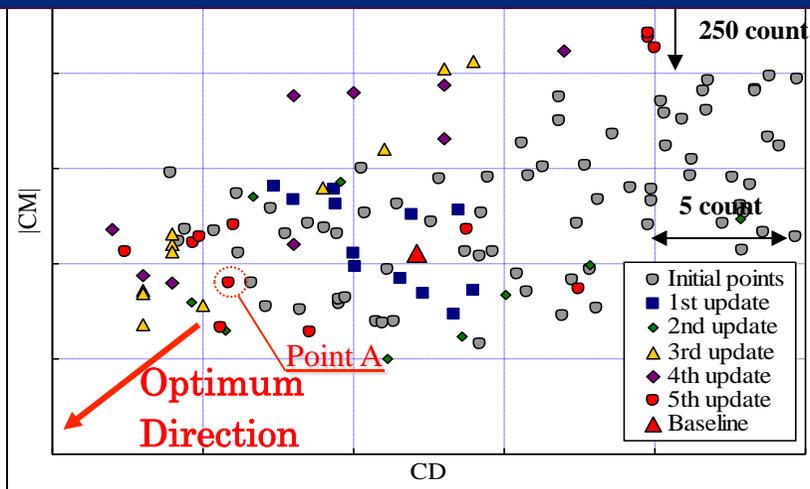
# MODE System for Regional Jet Design



# Comparison of Baseline Shape and Sample Points



Point A is improved by 6.2 counts in CD, 0.4 counts in  $\Delta$  CD, 79.4 counts in |CM|, and 74.0 kg in wing weight compared with the baseline



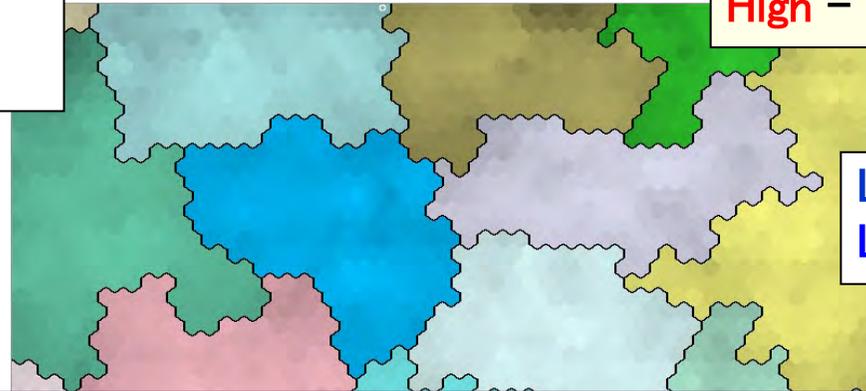
# Visualization of Design Space

(SOM made from the data uniformly distributed in design space)

High – Drag  
High – Pitching moment

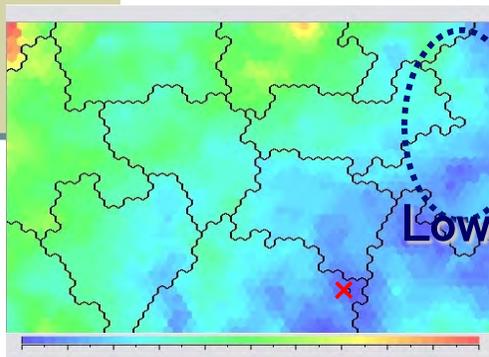
High – Drag divergence

Low – Pitching moment  
Low – Wing weight

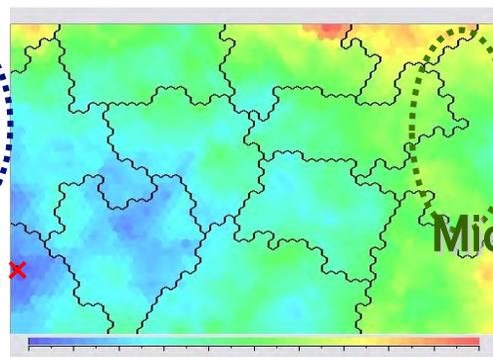


High – Wing weight  
Low – Drag

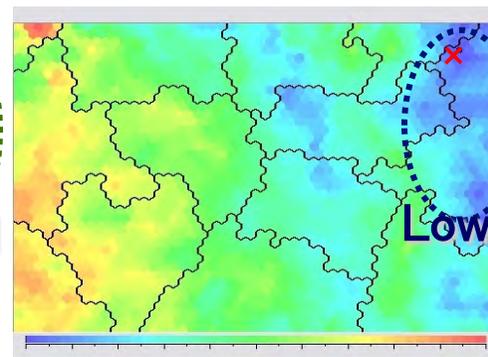
**If  $\Delta C_D$  is tolerable, this region is SWEET SPOT for design**



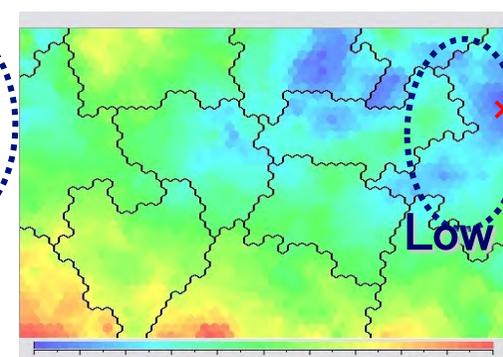
$C_D$



$\Delta C_D$



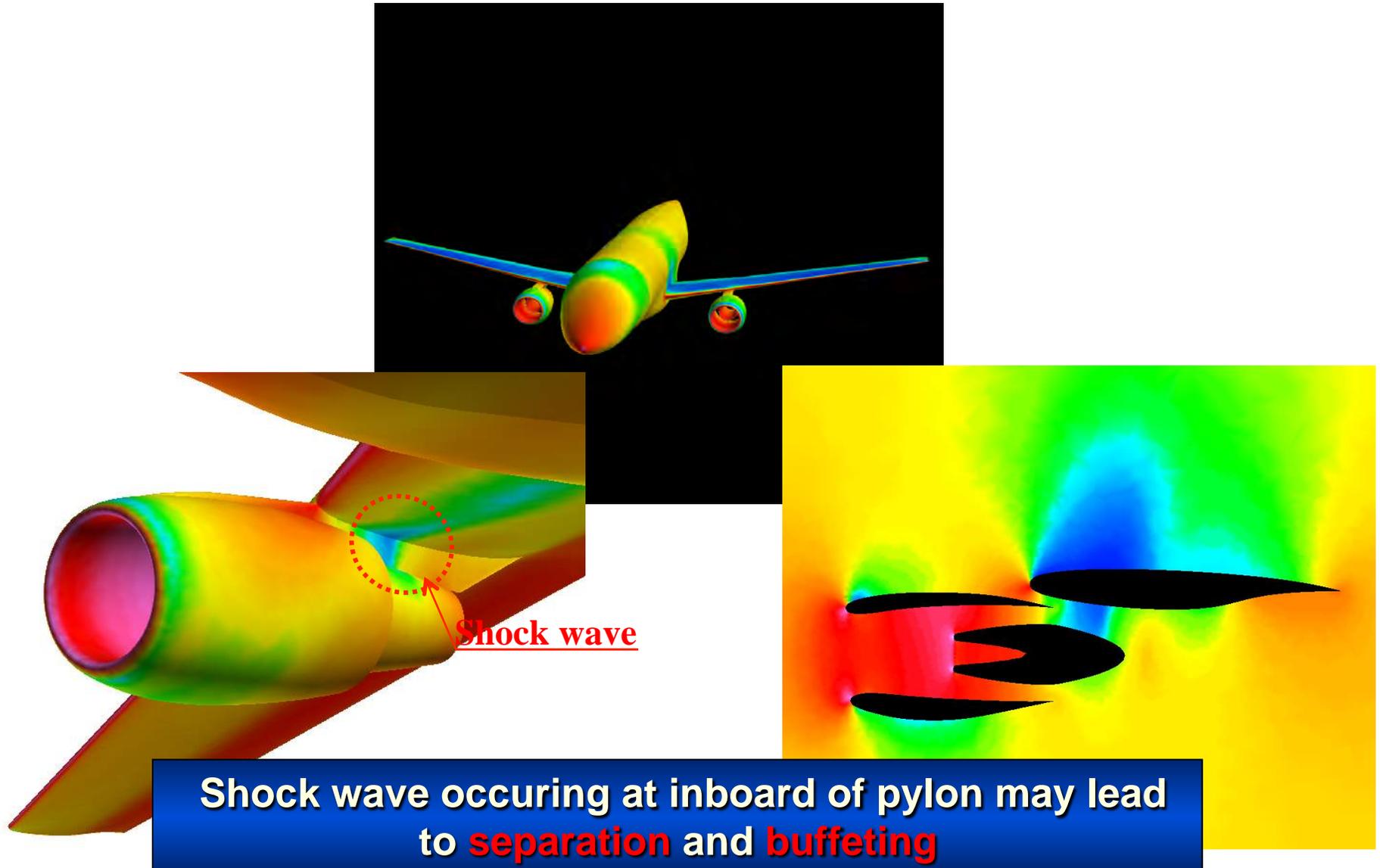
$|C_M|$



Wing weight

x : Minimum Point

# Optimization of Wing-Nacelle-Pylon-Body Configuration



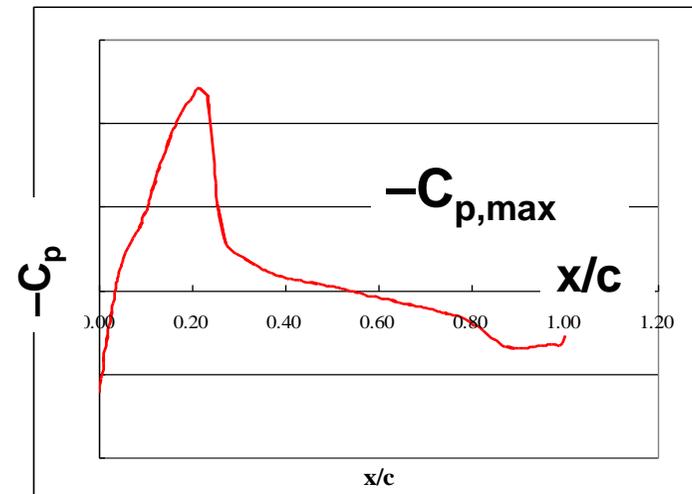
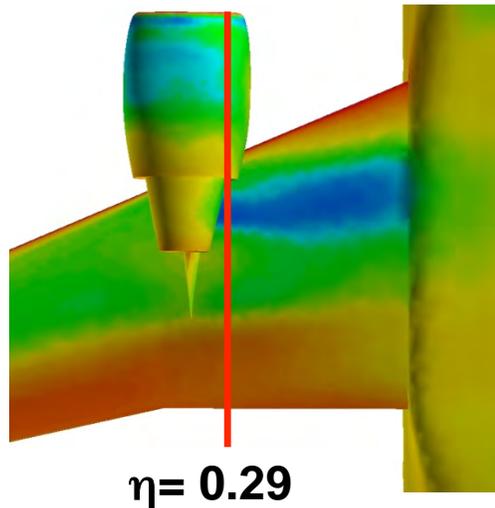
Shock wave occurring at inboard of pylon may lead to **separation** and **buffeting**

# Definition of Optimization Problem -1

## - Objective Functions -

### Minimize

1. **Drag** at the cruising condition ( $C_D$ )
  2. **Shock strength** near wing-pylon junction ( $-C_{p,max}$ )
  3. **Structural weight** of main wing (wing weight)
- ✓ Function evaluation tools
- CFD: Euler code (TAS-code)
  - CSD/Flutter analysis: MSC. NASTRAN

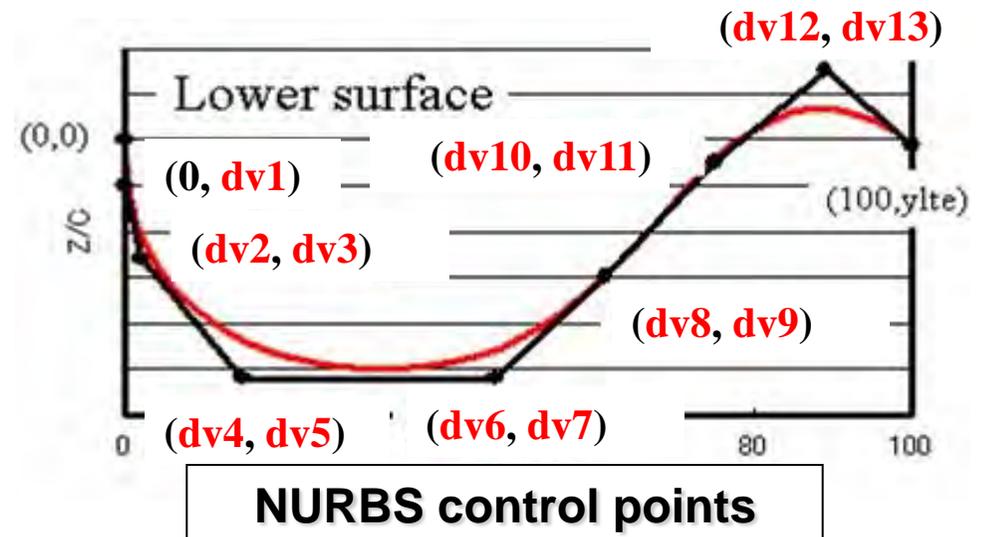
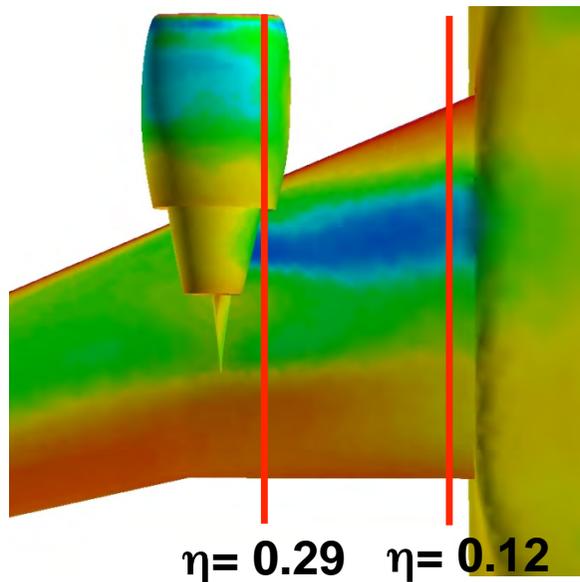


$-C_p$  distribution of lower surface @ $\eta=0.29$

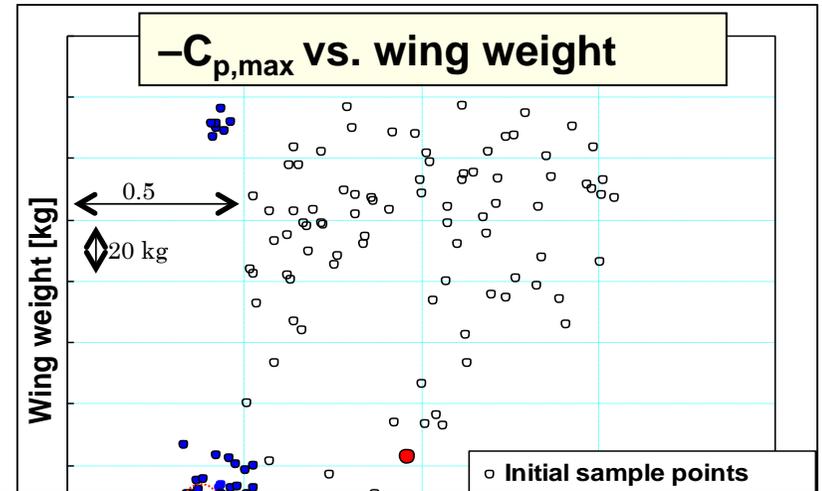
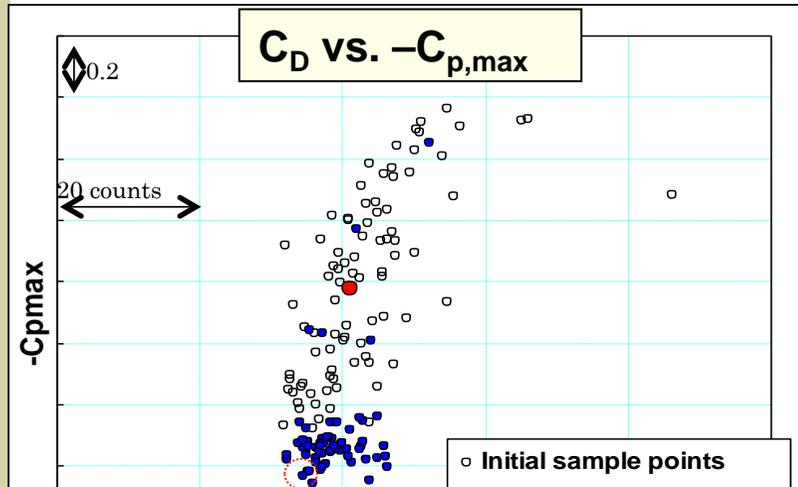
# Definition of Optimization Problem -2

## - Design Variables -

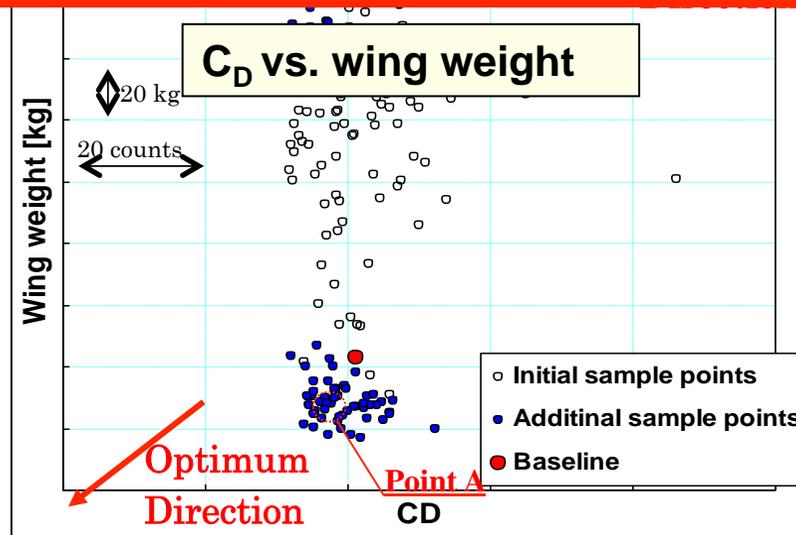
- Lower surface of Airfoil shapes at 2 spanwise sections  
 ( $\eta = 0.12, 0.29$ )  
 → 13 variables (NURBS)  $\times$  2 sections = 26 variables
  - Twist angles at 4 sections = 4 variables
- 30 variables in total**



# Comparison of Baseline Shape and Sample Points

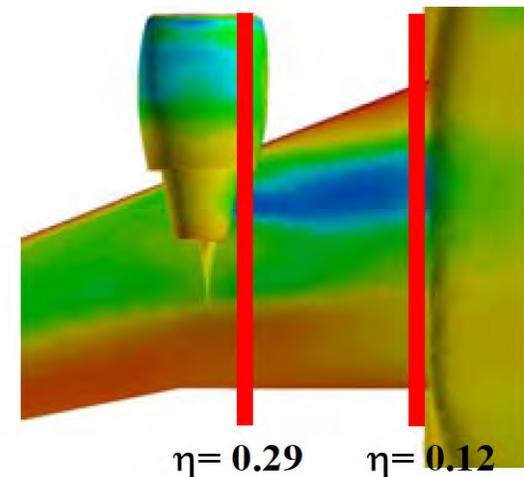
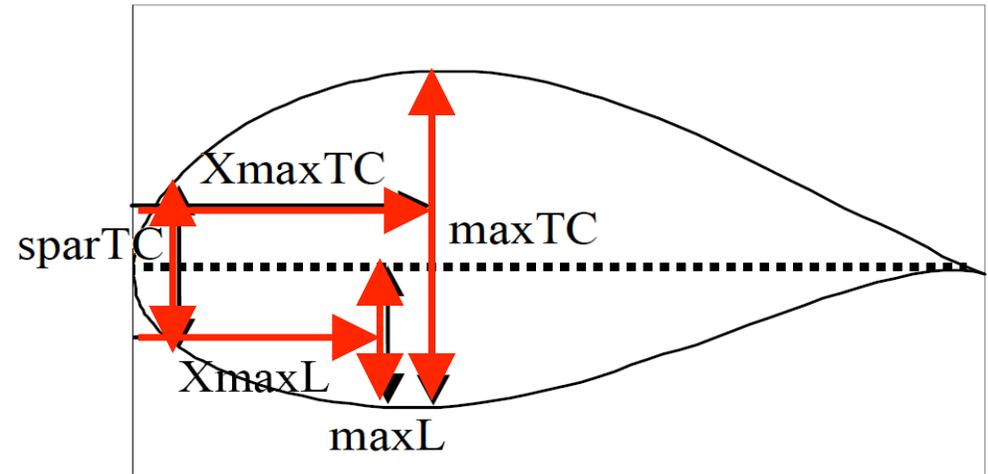


Point A is improved by 6.7 counts in  $C_D$ , 0.61 in  $-C_{p,max}$ , and 12.2 kg in wing weight compared with the baseline

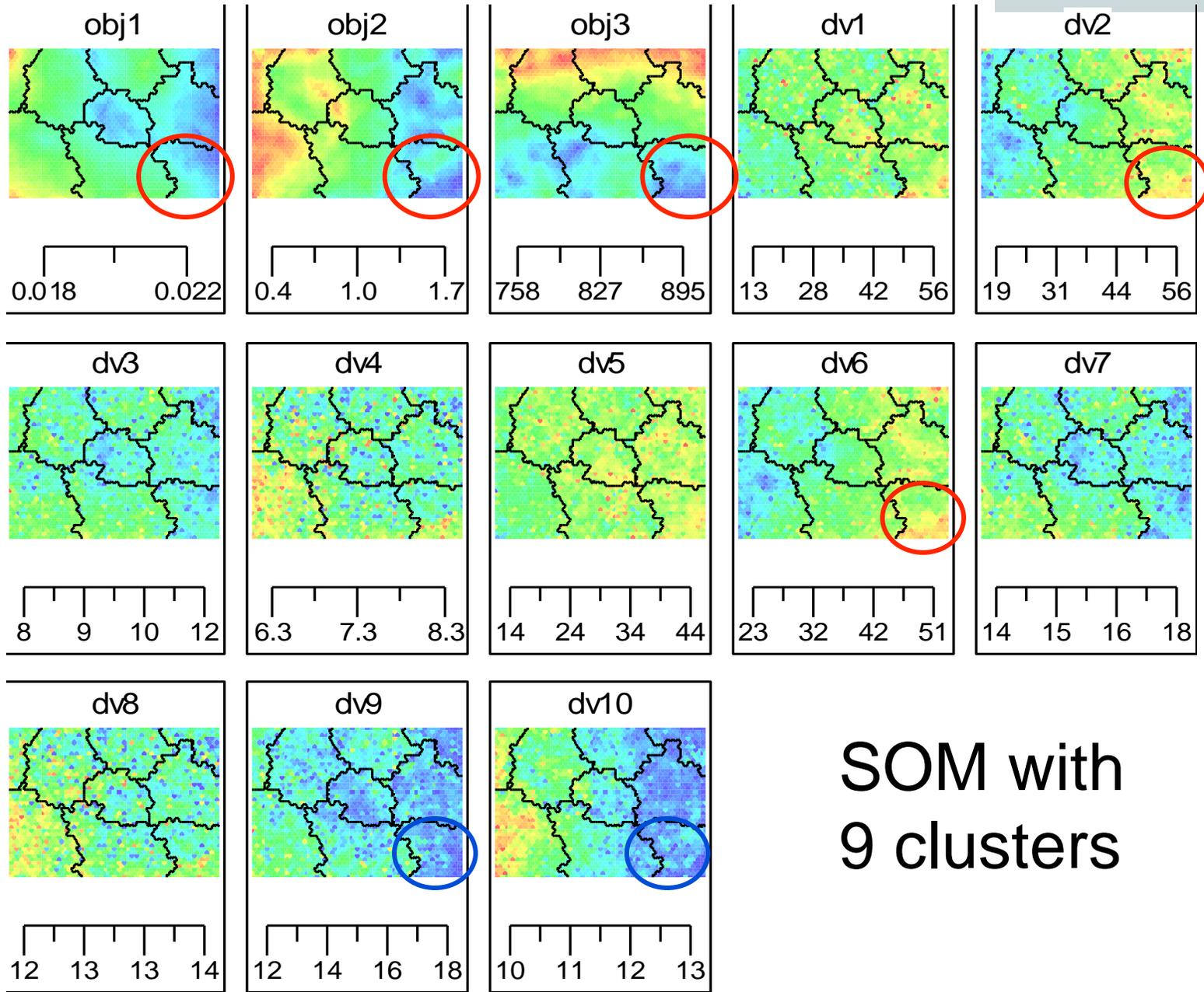


# Definition of Design Parameters for Data Mining

- XmaxL
- maxL
- XmaxTC
- maxTC
- sparTC
  - At wing root and pylon locations
  - 10 variables

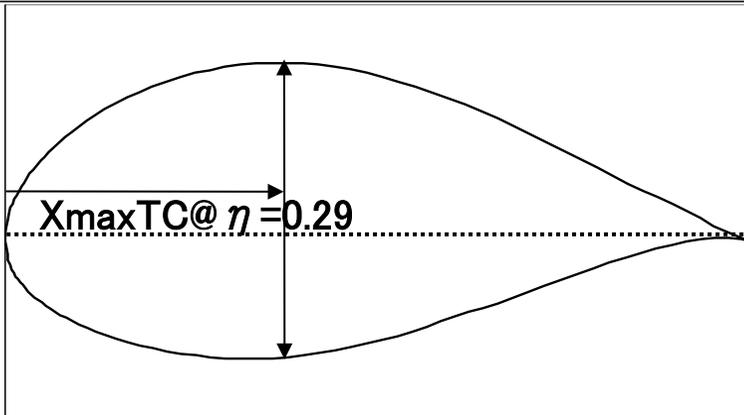
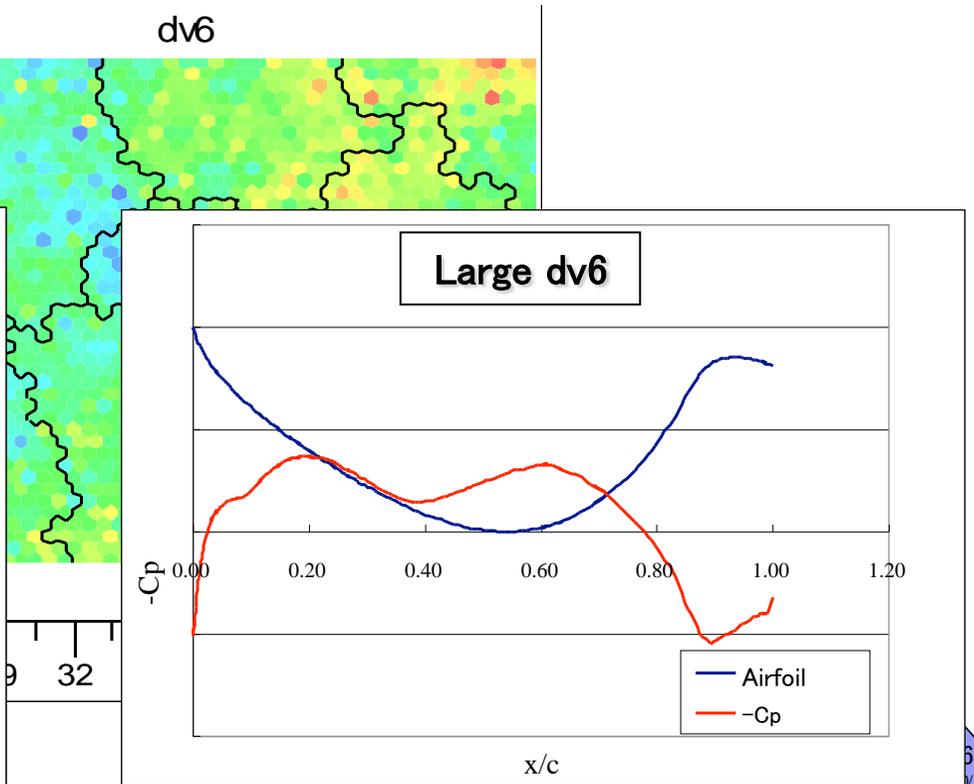
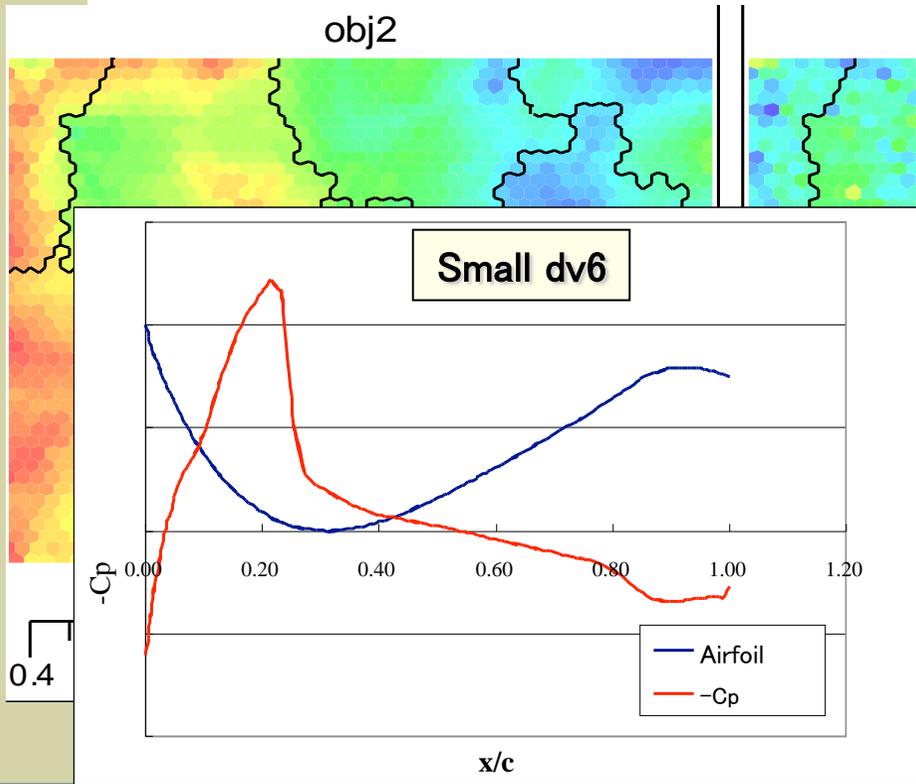


# Visualization of Design Space

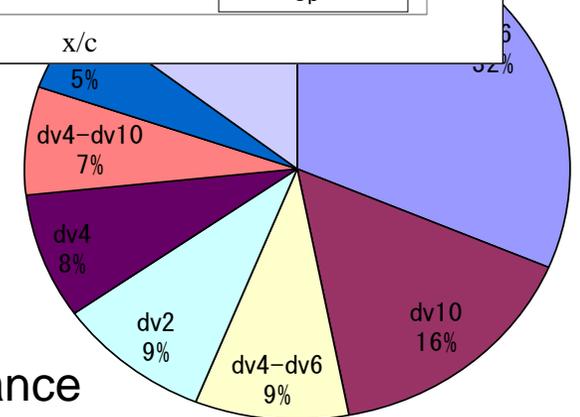


SOM with  
9 clusters

# -Cp,max and dv6 (XmaxTC at pylon)



Analysis of Variance (ANOVA)

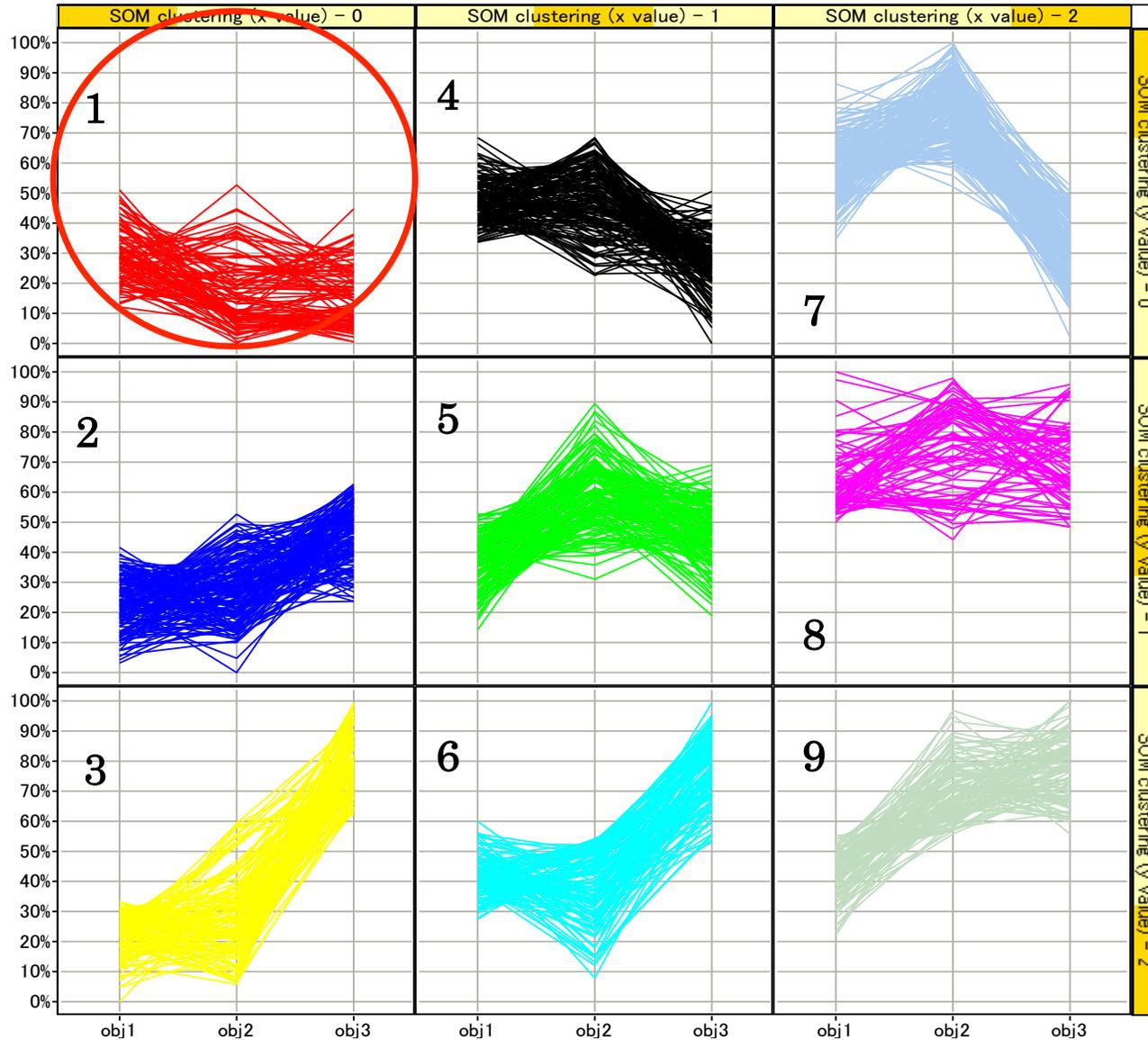


# *Analysis of Sweet–Spot Cluster*

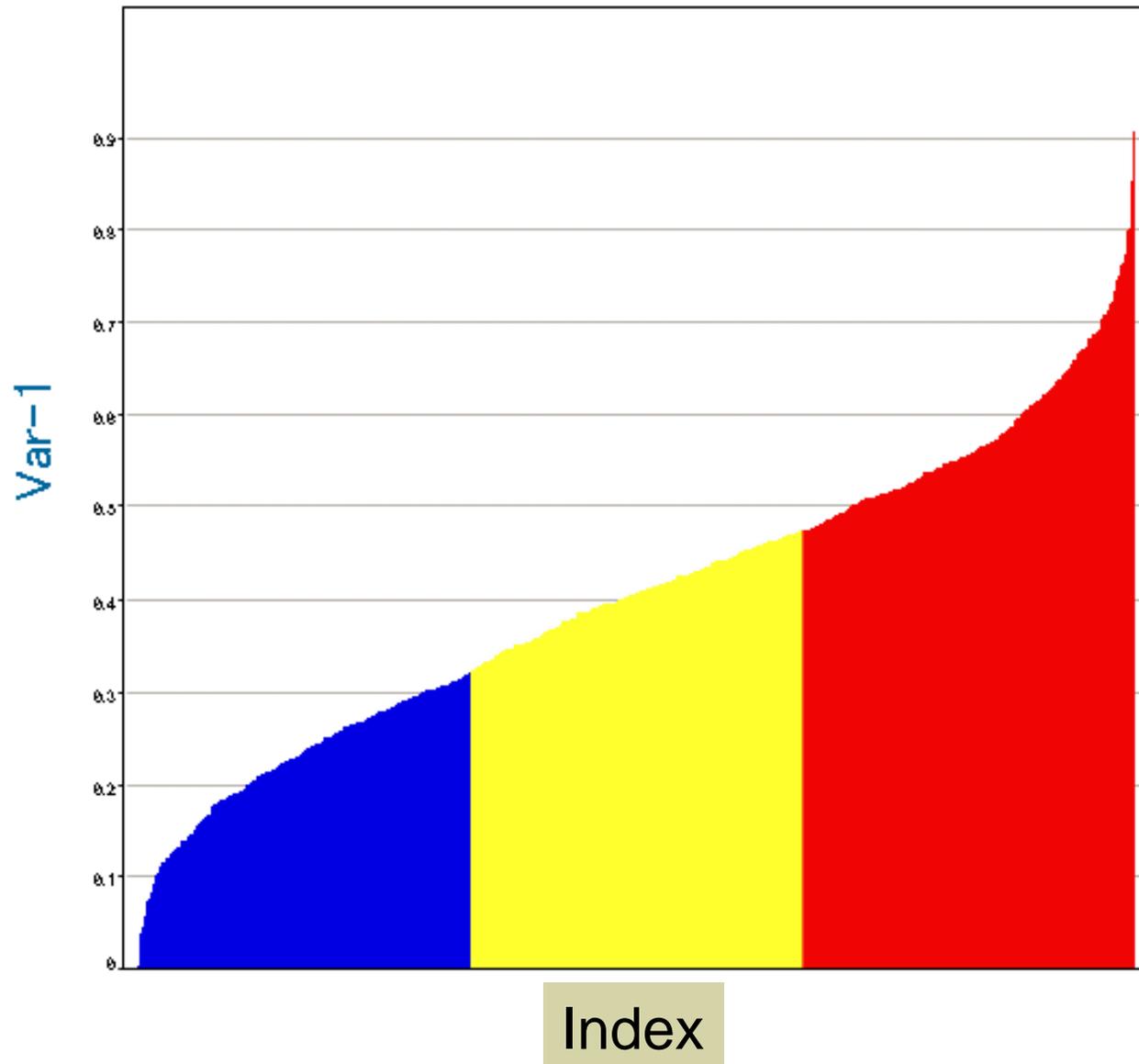
---

- Handpick
- Parallel coordinates
- Extraction of design rules by discretization of configuration variables
  - ✓ Visualization
  - ✓ Rough set

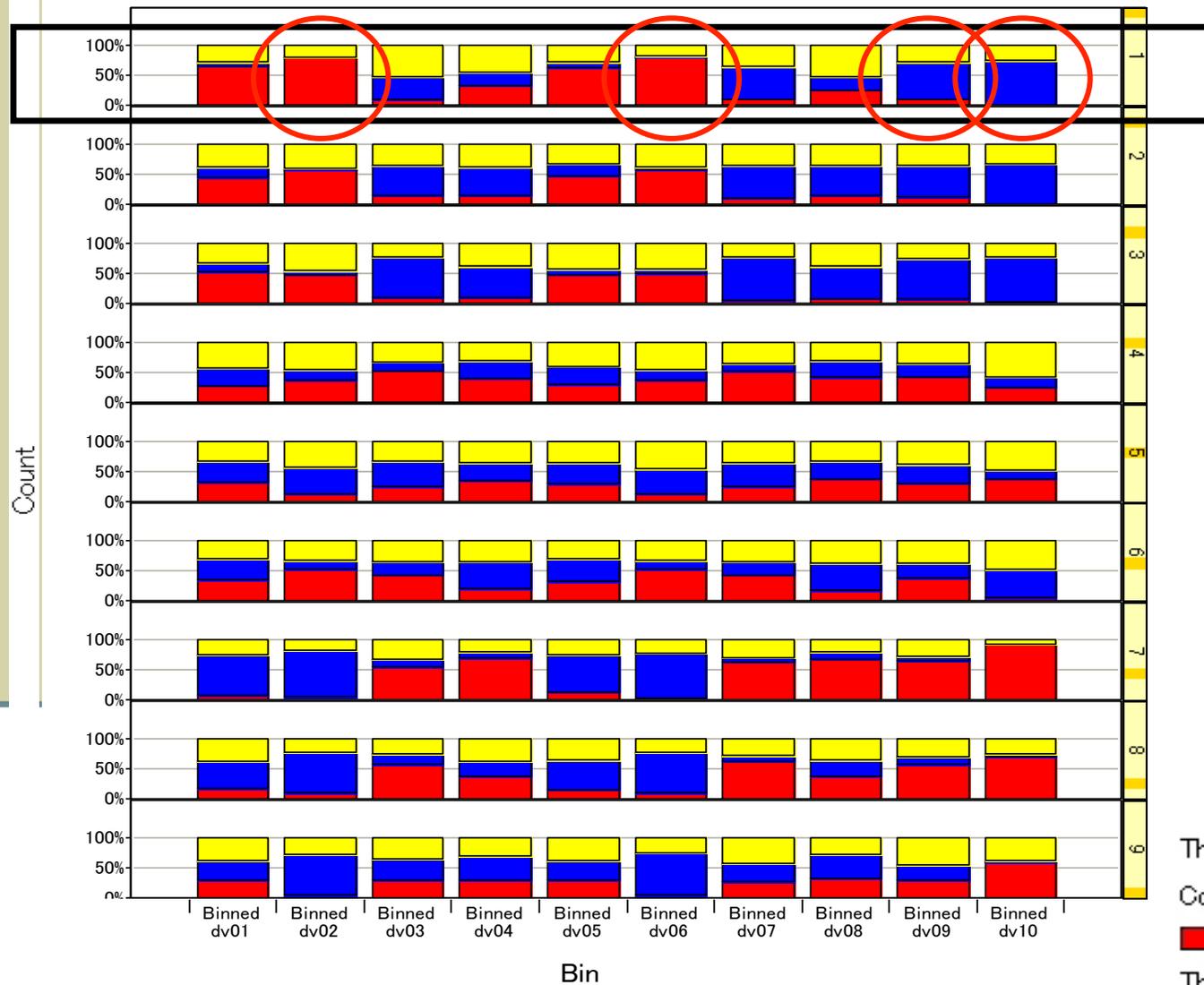
# Visualization of SOM Clusters by Parallel Coordinates



# *Discretization of Configuration Variables by Equal Frequency Binning*



# Finding Design Rules by Visualization



Sweet-spot cluster

|      | Airfoil parameters     |
|------|------------------------|
| dv2  | XmaxL @ $\eta = 0.29$  |
| dv6  | XmaxTC @ $\eta = 0.29$ |
| dv9  | sparTC @ $\eta = 0.12$ |
| dv10 | sparTC @ $\eta = 0.29$ |

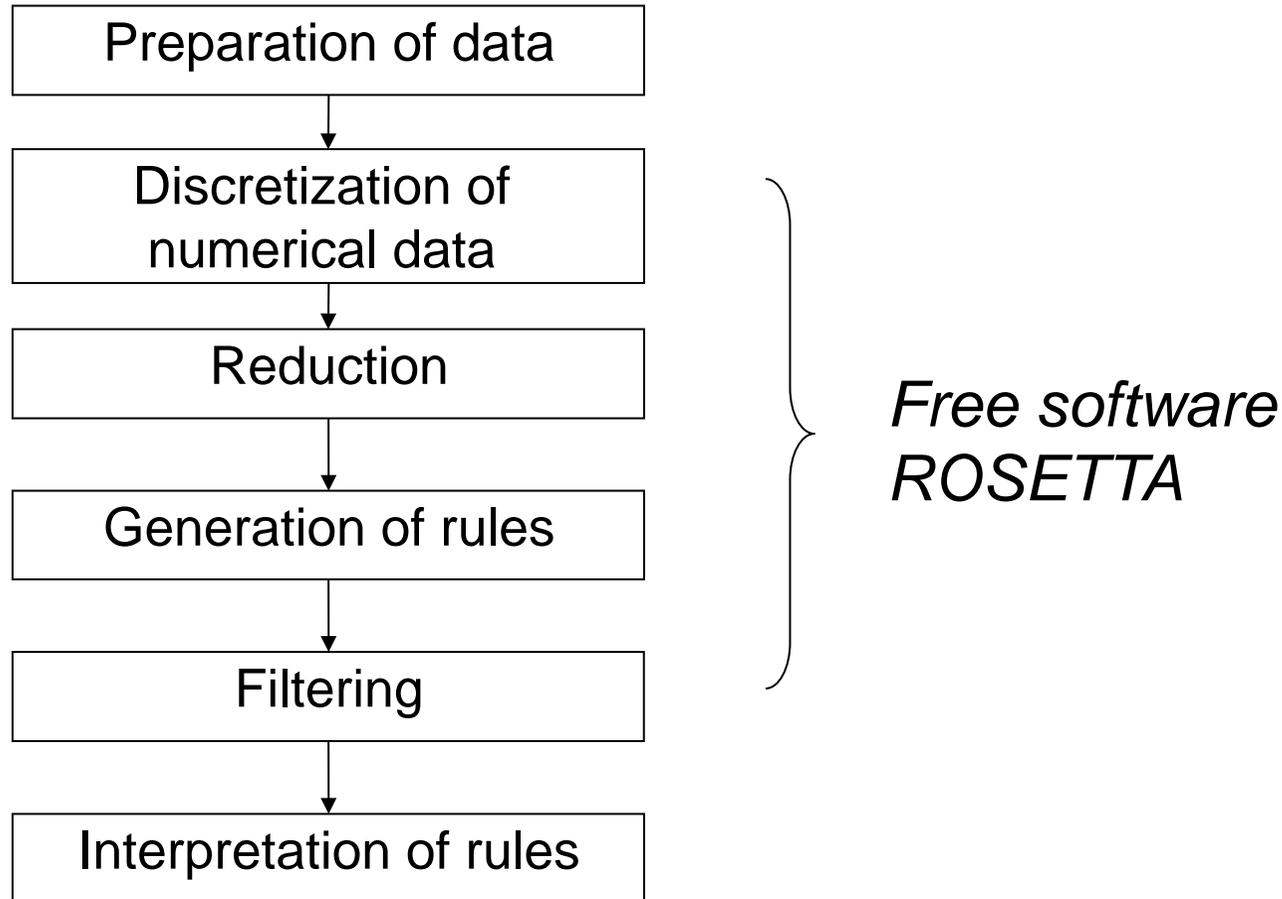
The height of a bar represents the number of records.

Color by Group:

High Low Middle

The labels show the height of each bar.

# Flowchart of Data Mining Using Rough Set



# Generated rules to belong to sweet spot cluster with support of more than eight occurrence

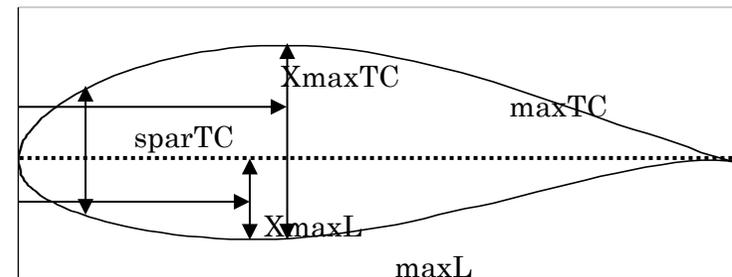
| Rule  | Count |
|---|-------|
| dv1([33.08, 39.30)) AND dv2([40.69, *)) AND dv5([29.65, 33.61)) AND dv7([15.09, 15.83)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                     | 10    |
| dv1([33.08, 39.30)) AND dv2([40.69, *)) AND dv3([8.88, 9.57)) AND dv5([29.65, 33.61)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                       | 10    |
| dv1([33.08, 39.30)) AND dv3([8.88, 9.57)) AND dv5([29.65, 33.61)) AND dv6([39.25, *)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                       | 10    |
| dv1([33.08, 39.30)) AND dv5([29.65, 33.61)) AND dv6([39.25, *)) AND dv7([15.09, 15.83)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                     | 10    |
| dv1([33.08, 39.30)) AND dv2([40.69, *)) AND dv5([29.65, 33.61)) AND dv6([39.25, *)) AND dv7([15.09, 15.83)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6) | 10    |
| dv1([33.08, 39.30)) AND dv3([8.88, 9.57)) AND dv4([7.54, *)) AND dv6([39.25, *)) AND dv10([*, 10.58)) => Cluster(C6)  | 9     |
| dv1([33.08, 39.30)) AND dv2([40.69, *)) AND dv3([8.88, 9.57)) AND dv4([7.54, *)) AND dv10([*, 10.58)) => Cluster(C6)  | 9     |
| dv3([8.88, 9.57)) AND dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv6([39.25, *)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |
| dv2([40.69, *)) AND dv3([8.88, 9.57)) AND dv5([29.65, 33.61)) AND dv8([12.82, 13.32)) AND dv9([*, 12.62)) => Cluster(C6)  | 8     |
| dv2([40.69, *)) AND dv5([29.65, 33.61)) AND dv7([15.09, 15.83)) AND dv8([12.82, 13.32)) AND dv9([*, 12.62)) => Cluster(C6)  | 8     |
| dv1([33.08, 39.30)) AND dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv7([15.09, 15.83)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |
| dv1([33.08, 39.30)) AND dv3([8.88, 9.57)) AND dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |
| dv1([33.08, 39.30)) AND dv4([7.54, *)) AND dv6([39.25, *)) AND dv7([15.09, 15.83)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                          | 8     |
| dv1([33.08, 39.30)) AND dv2([40.69, *)) AND dv4([7.54, *)) AND dv7([15.09, 15.83)) AND dv9([*, 12.62)) AND dv10([*, 10.58)) => Cluster(C6)                          | 8     |
| dv2([40.69, *)) AND dv3([8.88, 9.57)) AND dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |
| dv2([40.69, *)) AND dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv7([15.09, 15.83)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |
| dv4([7.54, *)) AND dv5([29.65, 33.61)) AND dv6([39.25, *)) AND dv7([15.09, 15.83)) AND dv10([*, 10.58)) => Cluster(C6)  | 8     |

# Statistics of rule conditions and comparison with previous results

|      | Sweet |
|------|-------|
| dv1  | 11    |
| dv2  | 9     |
| dv3  | 8     |
| dv4  | 10    |
| dv5  | 13    |
| dv6  | 7     |
| dv7  | 9     |
| dv8  | 2     |
| dv9  | 9     |
| dv10 | 14    |

| Number | Airfoil parameters     |
|--------|------------------------|
| dv1    | XmaxL @ $\eta = 0.12$  |
| dv2    | XmaxL @ $\eta = 0.29$  |
| dv3    | maxL @ $\eta = 0.12$   |
| dv4    | maxL @ $\eta = 0.29$   |
| dv5    | XmaxTC @ $\eta = 0.12$ |
| dv6    | XmaxTC @ $\eta = 0.29$ |
| dv7    | maxTC @ $\eta = 0.12$  |
| dv8    | maxTC @ $\eta = 0.29$  |
| dv9    | sparTC @ $\eta = 0.12$ |
| dv10   | sparTC @ $\eta = 0.29$ |

large  
 small

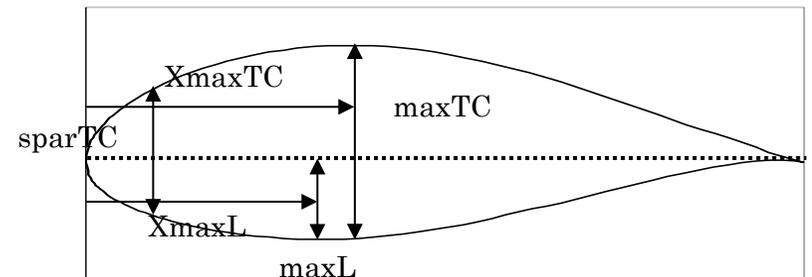


# Statistics of rule conditions for all objectives

|      | Sweet | Cd | Cp | WW |
|------|-------|----|----|----|
| dv1  | 11    | 1  | 1  | 5  |
| dv2  | 9     | 2  | 6  | 3  |
| dv3  | 8     | 5  | 6  | 4  |
| dv4  | 10    | 3  | 5  | 11 |
| dv5  | 13    | 8  | 1  | 7  |
| dv6  | 7     | 6  | 3  | 3  |
| dv7  | 9     | 5  | 6  | 5  |
| dv8  | 2     | 4  | 3  | 2  |
| dv9  | 9     | 2  | 2  | 3  |
| dv10 | 14    | 9  | 8  | 8  |

| Number | Airfoil parameters   |
|--------|----------------------|
| dv1    | XmaxL @ $\eta=0.12$  |
| dv2    | XmaxL @ $\eta=0.29$  |
| dv3    | maxL @ $\eta=0.12$   |
| dv4    | maxL @ $\eta=0.29$   |
| dv5    | XmaxTC @ $\eta=0.12$ |
| dv6    | XmaxTC @ $\eta=0.29$ |
| dv7    | maxTC @ $\eta=0.12$  |
| dv8    | maxTC @ $\eta=0.29$  |
| dv9    | sparTC @ $\eta=0.12$ |
| dv10   | sparTC @ $\eta=0.29$ |

large  
 small  
 No large dv10



# *Lessons Learned*

Designers do not like optimizer decides their design

- Optimal solutions are often unrealistic
  - Optimization problem is a model of actual design
- Optimization algorithms are continuously developed
  - A better solution will be obtained tomorrow

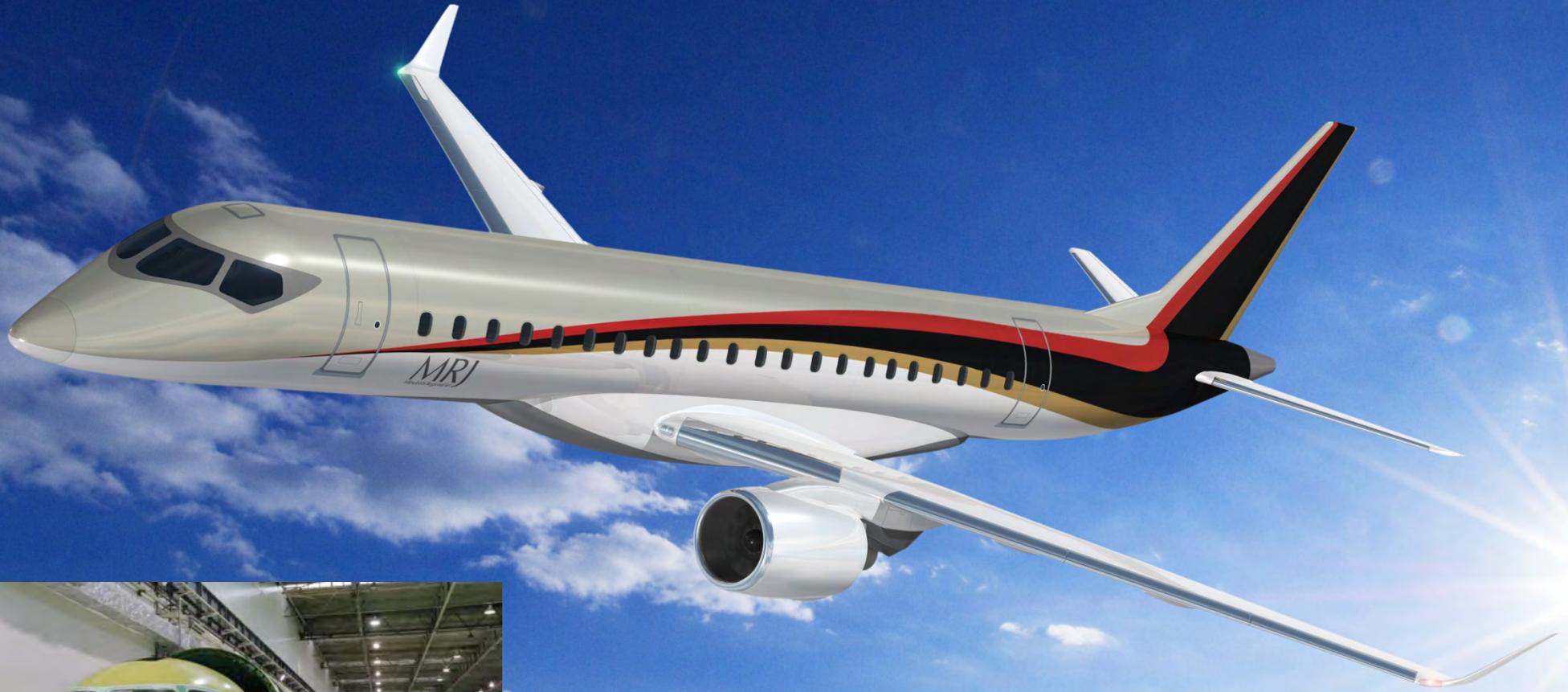
Designers need supports for their decisions

- Information about design space is desired
  - MODE has been proposed
- Visualization and data mining extract design knowledge
  - SOM has become an essential design tool

# *Acknowledgements*

- Mitsubishi Aircraft Corporation
- Mitsubishi Heavy Industries
- Supercomputer NEC SX-9 and SGI Altix-UV at Institute of Fluid Science
- Prof. Yasushi Ito, University of Alabama at Birmingham, for MEGG3D (mesh generator)
- Prof. Kazuhiro Nakahashi, Tohoku University, for TAS (unstructured-mesh flow solver)

Stay tuned for the first flight in 2015!



MRJ in production

謝謝